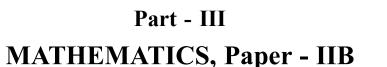
0293

Total No. of Questions - **37** Total No. of Printed Pages - **3**



(English Version)

MODEL QUESTION PAPER

(For the Academic year 2021-22 only)

Time : 3 Hours

Note: This question paper consists of three section A, B and C.

Section - A

I. Very short answer type questions.

- (i) Answer ANY TEN questions.
- (ii) Each question carries 2 marks.
- 1. If $ax^2 + bxy + 3y^2 5x + 2y 3 = 0$ represents a circle, find the values of *a* and *b*. Also find its radius and centre.
- 2. State the necessary and sufficient condition for lx + my + n = 0 to be a normal to the circle $x^2 + y^2 + 2gx + 2fy + c = 0$.
- 3. Find the pole of ax + by + c = 0 ($c \neq 0$) with respect to $x^2 + y^2 = r^2$.
- 4. Find the equation of the tangent to the circle $x^2 + y^2 4x 6y + 11 = 0$ at the point (3,4).
- 5. Find the angle between the circle $x^{2} + y^{2} 12x 6y + 41 = 0$ and $x^{2} + y^{2} + 4x + 6y 59 = 0$.
- 6. Find the equation of the common chord of the circles $x^2 + y^2 + 2x + 3y + 1 = 0$, $x^2 + y^2 + 4x + 3y + 2 = 0$.
- 7. Find the equation of the parabola whose focus is S(1, -7) and vertex is A(1, -2).

Turn Over

Max. Marks: 75

Regd.					
No.					

SET -

10×2=20

8. If the eccentricity of a hyperbola is $\frac{5}{4}$, then find the eccentricity of its conjugate hyperbola.

9. Evaluate:
$$\int \frac{1}{(x+3)\sqrt{x+2}} dx$$

10. Evaluate: $\int \sec^2 x \cdot \csc^2 x \, dx$

11. Evaluate:
$$\int \frac{6x}{3x^2 - 2} dx$$

12. Evaluate:
$$\int \frac{1}{1+\sin 2x} dx$$

13. Evaluate:
$$\int_{0}^{1} \frac{x^2}{x^2+1} dx$$

14. Evaluate:
$$\int_{0}^{\frac{\pi}{2}} \sec^4 \theta \, d\theta$$

15. Find the order and degree of the differential equation $\left(\frac{d^2y}{dx^2} - \left(\frac{dy}{dx}\right)^3\right)^{\frac{1}{2}} = 6y$.

Section - B

II. Short answer type questions.

- (i) Answer any FIVE questions.
- (ii) Each question carries four marks.
- 16. Show that the tangent at (-1, 2) of the circle $x^2 + y^2 4x 8y + 7 = 0$ touches the circle $x^2 + y^2 + 4x + 6y = 0$, also find its point of contact.
- 17. Find the angle between the tangents drawn from (3, 2) to the circle $x^{2} + y^{2} - 6x + 4y - 2 = 0$.
- 18. Find the length of the chord intercepted by the circle $x^2 + y^2 x + 3y 22 = 0$ on the line y = x 3.
- 19. Find the equation of the circle passing through the points of intersection of the circles $x^2 + y^2 8x 6y + 21 = 0$, $x^2 + y^2 2x 15 = 0$ and (1, 2).
- 20. Find the radical centre of the circles.

$$x^{2} + y^{2} - 2x + 6y = 0$$
, $x^{2} + y^{2} - 4x - 2y + 6 = 0$, $x^{2} + y^{2} - 12x + 2y + 3 = 0$.

- 21. Find the lengths of major axis, minor axis, latus rectum, eccentricity of the ellipse $9x^2 + 16y^2 = 144$.
- 22. If the length of the latus rectum is equal to half of its minor axis of an ellipse in the standard form, then find the essentricity of the ellipse.
- 23. Find the centre, eccentricity, foci, length of latus rectum for the hyperbola $4x^2 - 9y^2 - 8x - 32 = 0$.

24. Evalute:
$$\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{\cos x}{1+e^x} dx$$

25. Evalute:
$$\int_{0}^{\frac{\pi}{2}} \frac{\cos^{\frac{\pi}{2}} x}{\sin^{\frac{\pi}{2}} x + \cos^{\frac{\pi}{2}} x} dx$$

26. Solve:
$$\frac{dy}{dx} + 1 = e^{x+y}$$

27. Solve $\tan y \, dx + \tan x \, dy = 0$

Section - C

III. Long Answer type questions.

5×7=35

(i) Answer any FIVE questions.

(ii) Each question carries seven marks.

- 28. Show that the points (1, 1), (-6, 0), (-2, 2) and (-2, -8) are concyclic.
- 29. Find the direct common tangents to the circles $x^2 + y^2 + 22x 4y 100 = 0$; $x^2 + y^2 - 22x + 4y + 100 = 0$.
- 30. Show that the circles $x^2 + y^2 4x 6y 12 = 0$ and $x^2 + y^2 + 6x + 18y + 26 = 0$ touch each other, also find the point of contact and common tangent at this point of contact.
- 31. Show that the common chord of the circles $x^2 + y^2 6x 4y + 9 = 0$ and $x^2 + y^2 8x 6y + 23 = 0$ is a diameter of the second circle and also find its length.
- 32. If y_1, y_2, y_3 are the y-coordinates of the vertices of the triangle inscribed in the parabola $y^2 = 4ax$, then show that the area of the triangle is $\frac{1}{8a}|(y_1-y_2)(y_2-y_3)(y_3-y_1)|$ square units.
- 33. Evalute: $\int \sin x \cdot \sin 2x \cdot \sin 3x \, dx$

34. Evalute:
$$\int \frac{1}{\cos(x-a).\cos(x-b)} dx$$

35. Find:
$$\int \frac{1 - \tan x}{1 + \tan x} dx$$

36. Evalute:
$$\int_{0}^{1} \frac{\log(1+x)}{1+x^{2}} dx$$

37. Solve:
$$\frac{dy}{dx} = \frac{x - 2y + 1}{2x - 4y}$$